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2 **OPERATIONS OF A SHARED, AUTONOMOUS, ELECTRIC VEHICLE FLEET:**
3 **IMPLICATIONS OF VEHICLE & CHARGING INFRASTRUCTURE DECISIONS**
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5 T. Donna Chen
6 Assistant Professor
7 Department of Civil & Environmental Engineering
8 The University of Virginia
9 tdchen@virginia.edu

10
11 Kara M. Kockelman
12 (Corresponding author)
13 E.P. Schoch Professor of Engineering
14 Department of Civil, Architectural and Environmental Engineering
15 The University of Texas at Austin
16 kcockelm@mail.utexas.edu
17 Phone: 512-471-0210
18

19 Josiah P. Hanna
20 Department of Computer Science
21 The University of Texas at Austin
22 jphanna@cs.utexas.edu
23

24 **ABSTRACT**

25 There are natural synergies between shared autonomous vehicle (AV) fleets and electric vehicle
26 (EV) technology, since fleets of AVs resolve the practical limitations of today’s non-autonomous
27 EVs, including traveler range anxiety, access to charging infrastructure, and charging time
28 management. Fleet-managed AVs relieve such concerns, managing range and charging activities
29 based on real-time trip demand and established charging-station locations, as demonstrated in
30 this paper. This work explores the management of a fleet of shared autonomous (battery-only)
31 electric vehicles (SAEVs) in a regional discrete-time, agent-based model. The simulation
32 examines the operation of SAEVs under various vehicle range and charging infrastructure
33 scenarios in a gridded city modeled roughly after the densities of Austin, Texas.

34 Results indicate that fleet size is sensitive to battery recharge time and vehicle range, with each
35 80-mile range SAEV replacing 3.7 privately owned vehicles and each 200-mile range SAEV
36 replacing 5.5 privately owned vehicles, under Level II (240-volt AC) charging. With Level III
37 480-volt DC fast-charging infrastructure in place, these ratios rise to 5.4 vehicles for the 80-mile
38 range SAEV and 6.8 vehicles for the 200-mile range SAEV. SAEVs can serve 96 to 98% of trip
39 requests with average wait times between 7 and 10 minutes per trip. However, due to the need to
40 travel while “empty” for charging and passenger pick-up, SAEV fleets are predicted to generate
41 an additional 7.1 to 14.0% of travel miles. Financial analysis suggests that the combined cost of
42 charging infrastructure, vehicle capital and maintenance, electricity, insurance, and registration
43 for a fleet of SAEVs ranges from \$0.42 to \$0.49 per occupied mile traveled, which implies
44 SAEV service can be offered at the equivalent per-mile cost of private vehicle ownership for low
45 mileage households, and thus be competitive with current manually-driven carsharing services

46 and significantly cheaper than on-demand driver-operated transportation services. The
47 availability of inductive (wireless) charging infrastructure allows SAEVs to be price-competitive
48 with non-electric SAVs (when gasoline prices are between \$2.18 and \$3.50 per gallon).
49 However, charging SAEVs at attendant-operated stations with traditional corded chargers incurs
50 an additional \$0.08 per mile compared to wireless charging, and as such would only be price-
51 competitive with SAVs when gasoline reaches \$4.35 to \$5.70 per gallon.

52 **KEYWORDS**

53 Agent-based modeling, carsharing, electric vehicles, autonomous vehicles.

54 **INTRODUCTION**

55 Recent transportation trends in increasing electric vehicle (EV) sales and growing carsharing
56 membership have important impacts on greenhouse gas emissions and energy use. Incentivizing
57 plug-in EV adoption and shared-vehicle use may be key strategies for helping regions achieve
58 national- and state-level air quality standards for ozone and particulate matter, and ultimately
59 carbon-emissions standards. At the same time, with the rise of the shared-use economy,
60 carsharing is emerging as an alternative mode that is more flexible than transit but less expensive
61 than traditional private-vehicle ownership. However, the growth of EVs and carsharing are both
62 hindered by technological and social factors. For EVs, the most significant hindrance may be
63 “range anxiety,” a user’s concern for being stranded with a fully discharged battery and no
64 reasonable recharge option (Bartlett 2012). Meanwhile, as EVs penetrate the private and
65 commercial vehicle fleets, they are also gaining ground in the carsharing world. EVs are a
66 natural match for carsharing operations as existing members of carsharing operations tend to
67 drive smaller and more fuel efficient vehicles than non-carshare members (Martin and Shaheen
68 2011). Cutting edge carsharing operators (CSOs) are already employing EVs in their fleets (such
69 as Daimler’s Car2Go and BMW’s DriveNow operations), but the manual relocation of fleets in
70 one-way carsharing systems continues to present profitability challenges to CSOs. The
71 introduction of autonomous driving technology would remove the barrier of manual vehicle
72 relocation and presents a driver-free method for shared EVs to reach travelers’ origins and
73 destinations as well as charging stations. In a carsharing setting, a fleet of shared autonomous
74 electric vehicles (SAEVs) would automate the battery management and charging process, and
75 take range anxiety out of the equation for growth of EVs. With the recent popularity of on-
76 demand transportation services through transportation network companies, it is possible to
77 imagine a future travel system where autonomous vehicle (AV) technologies merges with
78 carsharing and EVs in a SAEV fleet. But can self-driving vehicles be shared, self-charged, and
79 right (battery-) sized for the trip lengths that travelers desire?

80 This study attempts to answer this question through the simulation of a SAEV fleet in a discrete-
81 time agent-based model, examining fleet operations in a 100-mile by 100-mile gridded
82 metropolitan area. Scenarios combine short-range and long-range electric vehicles with Level II
83 and Level III charging infrastructure to look at the impacts of vehicle range and charging time on
84 fleet size, charging station sites, ability to meet trip demand, user wait times, and induced vehicle
85 miles traveled (VMT). Following the discussion of the simulation results, a financial analysis
86 highlights the tradeoffs between capital investment in vehicles and charging infrastructure and
87 user benefits.

88 **PRIOR RESEARCH**

89 There is a wealth of literature examining carsharing, electric vehicles and charging infrastructure
90 planning, and autonomous vehicles as separate topics. Studies looking at gasoline-propelled and
91 (especially) electric AVs in a shared setting are more limited. Wang et al. (2006) proposed a
92 dynamic fleet management algorithm for shared fully automated vehicles based on queuing
93 theory. In a simulative environment with five stations and five vehicles, the average passenger
94 waiting time was 3.37 minutes with average vehicle usage rate of 4.3 vehicles per minute,
95 compared to a fixed dispatch algorithm where average passenger wait time was 4.89 minutes and
96 vehicle usage rate 3.7 vehicles per minute. Spieser et al. (2014) modeled a fleet of shared self-
97 driving vehicles in Singapore in the absence of any private vehicles, and found that each shared
98 vehicle can replace three privately owned vehicles and serve 12.3 households. In Kornhauser et
99 al. (2013), aTaxiStands (autonomous taxi stands) are placed in every half mile by half mile pixel
100 across New Jersey, and passengers walk to taxi stands rather than allowing AVs to relocate.
101 Douglas (2015) uses the base model proposed in Kornhauser et al. (2013) to size the fleet of an
102 autonomous taxi system in a 5-mile by 5-mile subset of the New Jersey model and found a
103 minimum of 550 vehicles was needed to serve the trip demand. Burns et al. (2013) examined the
104 performance of a shared autonomous fleet in three distinct city environments: a mid-sized city
105 (Ann Arbor, Michigan), a low-density suburban development (Babcock Ranch, Florida), and a
106 large densely-populated urban area (Manhattan, New York). The study found that in mid-sized
107 urban and suburban settings, each shared vehicle could replace 6.7 privately owned vehicles.
108 Meanwhile, in the dense urban setting, the current taxi fleet could be downsized by 30% with the
109 introduction of autonomous driving technology with average wait times at less than one minute.
110 The International Transport Forum (2015) looked at the application of shared and self-driving
111 vehicles in Lisbon, Portugal, and found that with ride-sharing enabled, each shared vehicle can
112 replace approximately 10 privately owned vehicles and induces 6% more VMT than the current
113 baseline. Without ride-sharing, each sequentially shared vehicle can replace 6 privately owned
114 vehicles but induces 44% more travel distance. This study also looked at the impact of
115 electrifying shared self-driving vehicles, assuming an electric range of 175 kilometers (108
116 miles) and a recharge time of 30 minutes, and found that the fleet would need to be 2% larger.
117 Fagnant and Kockelman (2014) presented an agent-based model for Shared Autonomous
118 Vehicles (SAVs) which simulated environmental benefits of such a fleet as compared to
119 conventional vehicle ownership and use in a dense urban core area. Simulation results indicated
120 that each SAV can replace 11 conventional private owned vehicles, but generates up to 10%
121 more travel distances. When the simulation was extended to a case study of low market
122 penetration (1.3% of trips) in Austin, Texas, each SAV was found to be able to replace 9
123 conventional vehicles and on average, generated 8% more VMT due to unoccupied travel
124 (Fagnant et al. 2015).

125
126 Charging/refueling in a fleet of shared self-driving vehicles has remained a missing component
127 in all of the prior studies mentioned here except ITF (2015) and Fagnant and Kockelman (2014),
128 both of which model the refueling process rather simplistically. Fagnant and Kockelman (2014)
129 modeled the logistics of refueling by assuming the 400-mile range SAVs could refuel at any
130 location within the grid with a fixed service lag time. In ITF (2015), recharging of EVs is only
131 looked at in terms of equivalent fleet sizing compared to longer-range and shorter-recharge-time,
132 gasoline-propelled vehicles. No study has examined the operations of shared autonomous
133 vehicles looking specifically at the vehicle propulsion system and charging infrastructure, both

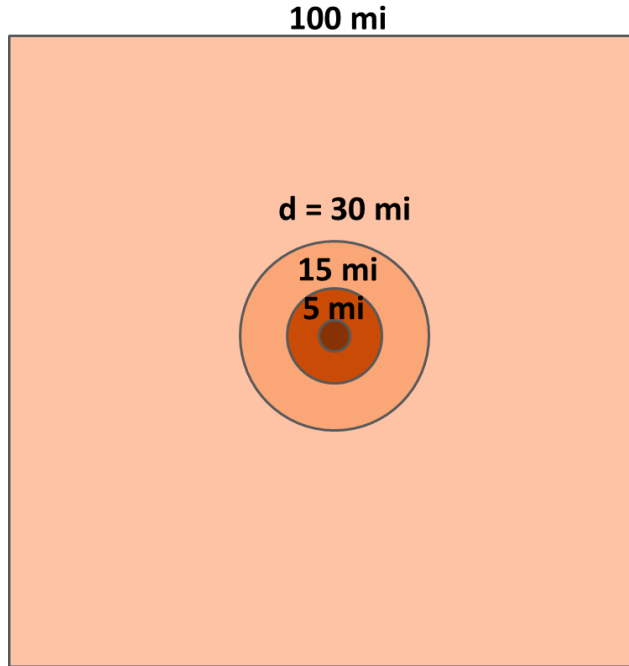
134 of which have direct impacts on the vehicle’s ability to travel to passengers as well as
135 fueling/charging stations. The work described here builds from the framework in Fagnant and
136 Kockelman (2014) and analyzes the operations of a SAEV fleet under different vehicle range and
137 charging infrastructure assumptions. There are natural synergies between AVs and EVs, as the
138 “smart” nature of AVs resolve the practical limitations of the non-autonomous EV in the market
139 today. These limitations include the previously discussed all electric range, charging station
140 density, and charging time management. Fleet managed “smart” AVs relieve such concerns from
141 the individual traveler, managing range and charging activities based on predicted trip demand
142 and established locations of charging stations, as demonstrated in the work here.

143 144 **METHODOLOGY**

145 146 **Model Setup**

147 The discrete-time agent based model used here is an expansion of the 10-mile by 10-mile model
148 proposed by Fagnant and Kockelman (2014). In its setup, the model generates a square 100-mile
149 by 100-mile gridded metropolitan area, divided into 160,000 quarter-mile by quarter-mile cells.
150 The gridded city (roughly modeled after the population density pattern of Austin, Texas) is
151 divided into four zones as shown in Figure 2-1: downtown (the innermost 2.5-mile radius), urban
152 (the next ring 7.5-mile radius), suburban (the next ring 15-mile radius), and exurban (the
153 remainder area). Zone population densities and trip rates are determined with data from the
154 Austin travel demand model segmented by population density (see Table 1). Each zone has its
155 own unique average trip generation rate (representing approximately 10% of all trips in the
156 Austin region inclusive of return trips, reflecting what Shaheen et al. [2006] estimates as market
157 potential for carsharing in a manually-driven setting) and average peak and off-peak travel
158 speeds (derived from sample peak and off-peak trips from the Austin travel demand model), as
159 shown in Table 1.

160



161

162

Figure 1. City Zones and Zone Limits

163

Table 1. Zone Trip Generation Rates & Travel Speeds

	Population Density (persons/mi ²)	Avg Trip Gen. Rate (trips/cell/day)	Travel Speed (mi/hr)	
			Peak	Off-Peak
Downtown	7500-50,000	129	15	15
Urban	2000-7499	39	24	24
Suburban	500-1999	11	30	33
Exurban	<499	1	33	36

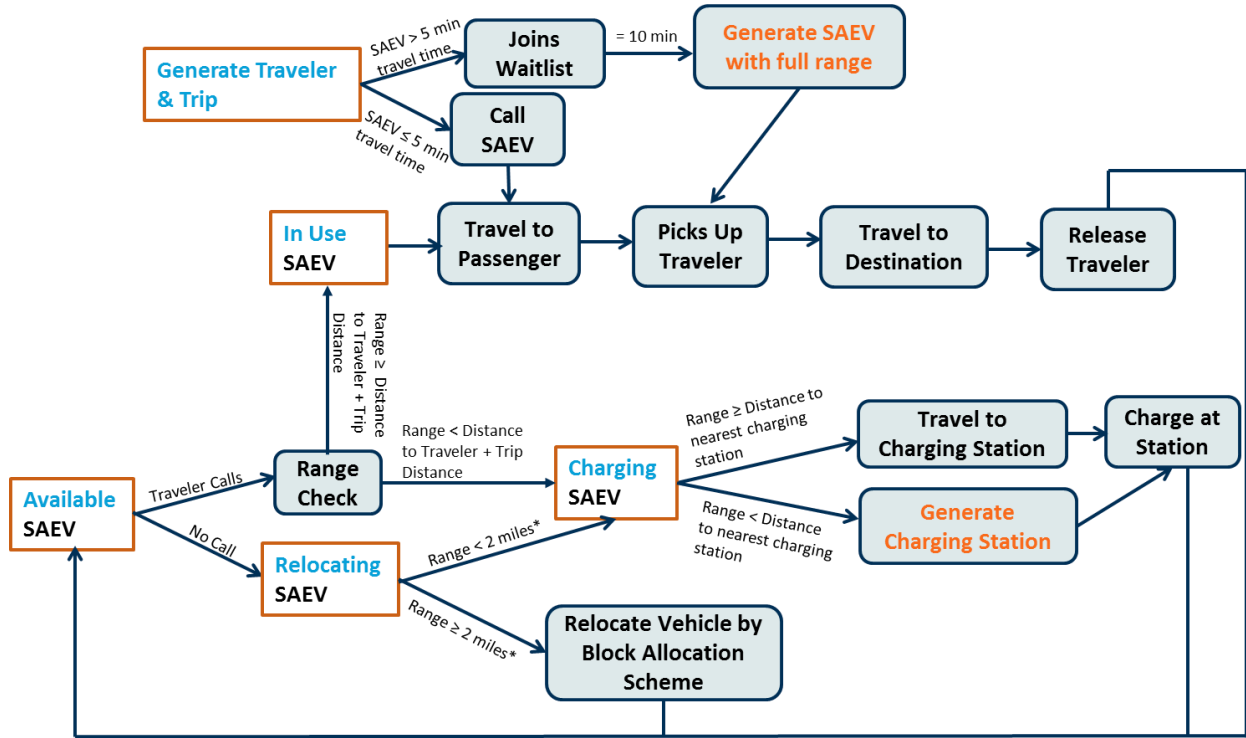
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165 The actual trip generation rate in each cell is drawn from a Poisson distribution with Table 1's
 166 value used as the average rate for each 5-minute time step within a 24-hour temporal distribution
 167 following the 2009 National Household Travel Survey (FHWA 2009). The destination cells for
 168 each trip generated are assigned as a function of the trip length (drawn from the 2009 NHTS trip
 169 length distribution) and proportional to the share of cells to the north, south, east, and west of the
 170 origin cells. In other words, the trip generation methodology used here favors higher attraction
 171 levels towards the city center. For detailed information on the step-by-step trip generation
 172 methodology used here, please refer to Fagnant and Kockelman (2014).

173 The model first runs through a two-phase warm start, during which the number of charging
 174 stations and the size of the SAEV fleet is determined. After the warm start completes, the model
 175 then runs for 50 consecutive days with the predetermined fleet size and charging station layout to
 176 output fleet operation performance metrics. Each phase of the model is discussed in detail in the
 177 following sections.

178 **Charging Stations Generation**

179 In Phase 1 of the warm start, consecutive 24-hour days are modeled to determine the number of
 180 charging stations needed for full service of the SAEV fleet. Figure 2 demonstrates the process of
 181 how and where charging stations are generated in the warm start.



182

183 **Figure 2. Agent Based Model Algorithm: Charging Station Generation**

184 Once a trip is generated by the process discussed in the Model Setup section, a traveler looks for
 185 the closest *available* status SAEV within a 5-minute travel time radius through a greedy search
 186 algorithm (searching at increasing distances starting from its own origin cell). If an available
 187 SAEV is located within a 5-minute travel-time radius, the traveler claims the SAEV and the
 188 SAEV falls under *in use* mode for the subsequent time periods to pick up the traveler, complete
 189 the assigned trip, and release traveler. If a SAEV is not available within a 5-minute travel-time
 190 radius, the traveler joins a waitlist. In the following 5-minute time step, travelers on the wait list
 191 are prioritized and served first, before new trips generated during the current time step are served
 192 by SAEVs. When a traveler has been on the waitlist for 10 minutes (or two time steps), a new
 193 SAEV is generated with full charge in the traveler’s origin cell.

194 Once a SAEV releases a traveler at the destination cell, the vehicle changes from *in use* to
 195 *available* status, and awaits for a traveler call in the subsequent 5-minute time step. If the vehicle
 196 is not called in the time step, the SAEV changes from *available* to *relocating* status, and its
 197 subsequent actions are discussed in the Strategic Vehicle Relocation section. If a traveler calls,
 198 the SAEV checks to ensure that its remaining range is greater than the distance to the traveler
 199 plus the distance of the requested trip before accepting the call. If the range is insufficient, the
 200 call is rejected and the SAEV changes from *available* to *charging* status. In *charging* status, the

201 SAEV looks for the nearest charging station (by the same greedy algorithm used in trip
 202 matching), and if one does not exist within its remaining range, a charging station is generated in
 203 the SAEV's current cell. The SAEV then stays in *charging* status at the charging station for the
 204 number of time steps proportional to its remaining range to achieve full charge status, as shown
 205 in Equation 1:

$$206 \quad T_{charge} = \left\lceil \frac{Range_{full} - Range_{current}}{Range_{full}} \right\rceil T_{full} \quad (1)$$

207 where T_{charge} is the number of time steps a SAEV remains at the charging station in *charging*
 208 status before becoming *available* for the next traveler, $Range_{full}$ is the number of grid cells a
 209 SAEV can travel when fully charged, $Range_{current}$ is the SAEV's current remaining range, and
 210 T_{full} is the number of time steps required for a fully depleted SAEV battery to fully charge.
 211 Phase 1 continues until the number of charging stations on consecutive days converges to within
 212 1%.

213 **SAEV Fleet Generation**

214 When Phase 1 is complete, the charging station layout is set and no more charging stations can
 215 be added to the city. The SAEV fleet is cleared to start Phase 2, which determines the size of the
 216 SAEV fleet. The two phases of the warm start operate independently of each other since the
 217 number of SAEVs required in the fleet depends on the number of charging stations available.
 218 During the generation of the charging stations, the corresponding SAEV fleet is (temporarily)
 219 oversized. The overall algorithm for Phase 2 is similar to that of Phase 1. However, because no
 220 charging stations are generated in Phase 2, in order to accept a traveler's call, the SAEV must
 221 have sufficient range to travel to the traveler, complete the requested trip, and travel to the
 222 nearest charging station from the destination cell. Phase 2 is run for 20 days, with vehicles
 223 cleared at the end of each day. The average number of SAEVs generated from the 20 days is
 224 taken as the fleet size for the full run.

225 **Waitlist**

226 Once the charging station locations and SAEV fleet size is determined from the two-phase warm
 227 start, the program runs through 50 consecutive days when vehicles are in continuous operation
 228 (no vehicle clearing). The full run's model structure is identical to that of Phase 2, except no new
 229 SAEVs are generated and travelers remain on the waitlist. If a traveler's trip request is rejected in
 230 6 consecutive time steps (equivalent to 30 minutes on the waitlist), that trip is considered
 231 unserved and is removed from the waitlist.

232 **Strategic Vehicle Relocation**

233 During each step of the model (warm start and full run), available SAEVs that are not called by
 234 travelers are assigned to *relocating* status for that time step. The relocation strategy used in this
 235 model first attempts to balance the available SAEVs in the current time step with the expected
 236 demand in a 2-mile by 2-mile block in the subsequent time step, then uses two additional
 237 strategies to efficiently distribute SAEVs amongst bordering blocks with a large vehicle supply
 238 gap. This combination of relocation strategies was deemed the most effective out of several that

239 were tested in Fagnant and Kockelman (2014), which also describes the relocation process in
 240 detail. To ensure that vehicles in *relocating* status have sufficient range for relocation, a check
 241 ensures that the SAEV has sufficient range to travel a distance equivalent to 5 minutes of travel
 242 time from its original cell (roughly equivalent to 2 miles but varies slightly with zone) plus the
 243 distance to the nearest charging station to the relocation destination.

244
 245 **MODEL SCENARIO RESULTS**

246 The agent-based model described here is run for several scenarios to examine the sensitivity of
 247 various fleet operation metrics to model inputs, as shown in Table 2. A non-electric SAV
 248 scenario (assuming 400-mile range and 15 minute refueling time) is run as a reference case for
 249 comparison to the results in Fagnant and Kockelman (2014). Next, the SAEV scenario assumes
 250 the vehicle has an 80-mile range (similar to current models of the Nissan Leaf, Chevrolet Spark,
 251 Honda Fit EV, and BMW i3) and 4 hour recharge time, corresponding to charging times of
 252 current market BEVs with a 240-volt AC Level II charger. A SAEV Fast Charge scenario
 253 combines the same 80-mile vehicle with a recharge time of 30 minutes, mimicking the
 254 specifications of current market BEVs with a Level III 480-volt DC high-current charger.
 255 Following fast charging guidelines, the SAEVs in the fast charge scenarios will only be charged
 256 to 80% full to protect the batteries from losing capacity with repeat fast charging, which
 257 effectively reduces the range to 64 miles. The last two scenarios looks at various types of
 258 charging in combination with long-range BEVs matching the 200-mile range specification of the
 259 upcoming Chevrolet Bolt and Tesla Model 3 (both with 2017 planned release dates). The LR
 260 SAEV scenario combines a 200-mile range with a 4-hour recharge time while the LR SAEV Fast
 261 Charge scenario combines a 160-mile effective range with a 30 minute fast charge time.

262 **Table 2. Scenario Results**

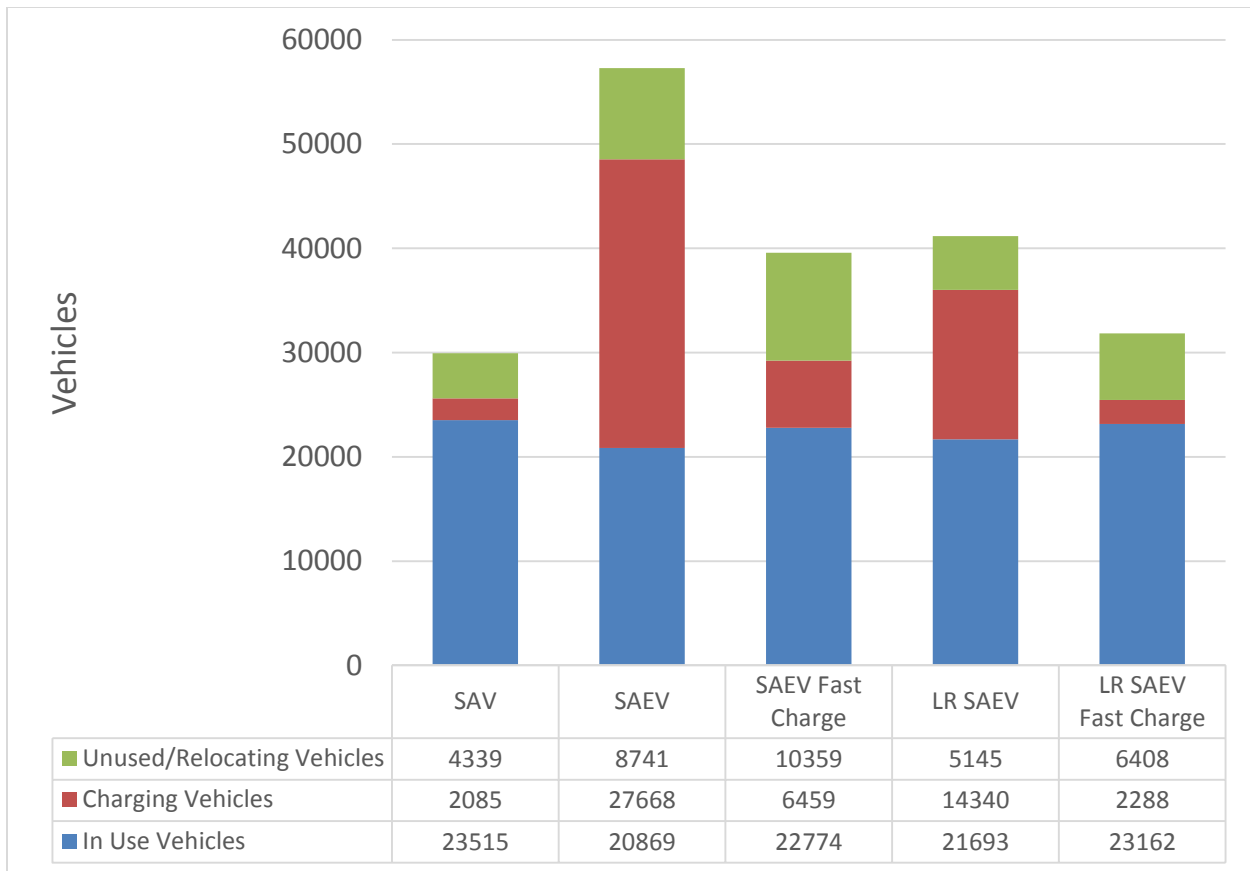
Scenario	SAV	SAEV	SAEV Fast Charge	LR SAEV	LR SAEV Fast Charge
Range (mi)	400	80	64	200	160
Refuel/Recharge Time (min)	15	240	30	240	30
# of Charging/Fueling Station Sites	1062	1562	1573	1555	1517
Fleet Size	29,939	57,279	39,593	41,179	31,859
Avg Daily Miles per Vehicle	259	131	197	190	241
Avg Daily Trips per Vehicle	22.3	11.4	16.9	16.3	20.8
Private Veh Replacement Rate	7.32	3.73	5.53	5.33	6.82
% Trips Unserved	2.13%	3.94%	4.36%	2.29%	2.73%
Avg Trip Distance (mi)	10.1	9.41	9.08	10.0	10.0
Avg Wait Time Per Trip (min)	9.3	8.1	7.7	8.4	9.5
Avg Range Remain. at Recharge (mi)	1.6	43.1	40.7	5.4	2.5
% Total Unoccupied Travel	6.6%	10.7%	14.0%	7.1%	7.1%
% Unoccupied Travel for Trips	5.2%	4.1%	3.0%	4.7%	4.9%
% Unoccupied Travel for Charging	0.3%	2.5%	5.0%	0.6%	0.7%
% Unoccupied Travel for Relocation	1.1%	4.1%	6.1%	1.9%	1.4%
Max % of Concurrent Charging	7.5%	52.6%	41.7%	40.2%	7.5%

Vehicles					
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264 Simulation results show that the number of vehicles needed in a fleet is highly sensitive to charge
 265 time and, to a slightly lesser degree, vehicle range. Substituting Level III in place of Level II
 266 chargers for SAEV and LR SAEV fleets reduced the required fleet size by 30.9 and 23.3%,
 267 respectively. On the other hand, increasing the electric range of vehicles from 80 to 200 miles
 268 reduced the fleet size by 28.1 and 19.5% respectively for Level II and Level III charging
 269 schemes. Combining these effects, the necessary fleet for the SAEV scenario is almost double
 270 the size of that for the LR SAEV Fast Charge scenario. Using 2009 NHTS rates for 3.02 private
 271 car trips per licensed U.S. driver and 0.99 household vehicles per licensed driver (Santos et al.
 272 2011), the private vehicle replacement rate is highest at one shared vehicle for every 7.3 private
 273 vehicles in the SAV scenario, in line with the results from the mid-sized urban and suburban
 274 models in Burns et. al (2013) and the regional model in Fagnant and Kockelman (2015).
 275 However, once the fleet is electrified, the private vehicle replacement rate ranges from a
 276 comparable 1:6.8 vehicle ratio in the LR SAEV Fast Charge scenario to a much lower 1:3.7
 277 vehicle ratio in the SAEV scenario. Non-electric SAV fleet requires the fewest number of
 278 vehicles (29,939) for full service, and the closest competitive EV scenario (LR SAEV Fast
 279 Charge) increases that fleet size by 6.6%, a slightly larger difference than estimated in ITF
 280 (2015) despite longer EV range assumption. As seen in Figure 3, a snap shot of each vehicle's
 281 activity during the peak 5-minute period (defined as the time step with the most *in use* vehicles)
 282 demonstrates that with longer charging times and shorter ranges, vehicles are simply tied up at
 283 charging stations not able to service trip demand. While the number of *in use* vehicles is
 284 relatively consistent across all scenarios, the number of *charging* vehicles increases significantly
 285 with longer vehicle charge times and shorter electric range.

286



287

288

Figure 3. Peak (5-Minute) Period Vehicle Use

289 As seen in the results in Table 2, for full service, all EV scenarios produced similar numbers of
 290 charging station sites. This result suggests that the number of charging station sites (cells with
 291 charging stations) necessary for full service has an inelastic relationship with the vehicle’s
 292 electric range, but is more determined by the geography of the city (or size of the service geo-
 293 fence). Conversely, the total number of chargers needed (as proxied by the average number of
 294 charging vehicles in the time step with the most concurrent charging across 50 days) is highly
 295 sensitive to charge time and vehicle range. Using Level III chargers cuts the charge time for
 296 SAEV and LR SAEV fleets by 87.5%, and correspondingly, the number of needed chargers by
 297 45.2 and 85.6%. Holding charging infrastructure constant, substituting LR SAEVs for SAEVs in
 298 the fleet (and increasing vehicle range by 150%), the number of chargers needed decreases 45.0
 299 and 85.6%. Generally speaking, high trip demand periods coincide with high charging activity
 300 periods. Simulation results suggest that the LR SAEV Fast Charge scenario is best at spreading
 301 out charging demand across the day, with a maximum of 7.46% of vehicles in the fleet
 302 concurrently charging during any time step. On the other hand, in the base SAEV scenario, as
 303 many as 52.6% of the vehicle fleet charge concurrently during the peak charge time period of the
 304 day.

305 Simulation results show that longer vehicle range translates into higher percentages of trips
 306 served, as vehicles simply cannot serve trips longer than its maximum range. In the 2009 NHTS,
 307 1.05% of the trips are over 80 miles long. In the simulation results, the difference between trips

308 served between the 200-mile LR SAEV and the 80-mile SAEV is 1.65%. However, longer
 309 vehicle range is generally associated with longer wait times in the simulation results, primarily
 310 due to the inefficiency of serving trips originating in low-demand suburban and exurban areas a
 311 shared setting. As seen in Table 2, longer-range vehicles spend more of their “empty” VMT for
 312 passenger pick-up while shorter-range vehicles spend more of their “empty” VMT for relocation.

313 Each autonomous driving scenario produced an additional 7.1 to 14.0% of unoccupied VMT, in
 314 line with estimates in ITF (2015) and Fagnant et al. (2015). As seen in Table 2, for vehicles with
 315 longer range (SAVs and LR SAEVs), the greatest portion (65.6 to 78.4%) of that induced travel
 316 can be attributed to unoccupied vehicles traveling to pick up passengers. Unoccupied travel to
 317 charging/refueling stations played a relatively minor role in inducing additional VMT, summing
 318 to 0.5 to 0.7% of total VMT (or 4.5 to 10.0% of “empty” miles traveled) for longer range
 319 vehicles, as seen in Figure 4. Due to the more frequent need to recharge, induced miles traveled
 320 for recharging is greater for scenarios with shorter range vehicles. SAEVs registered an
 321 additional 2.5 to 5.0% miles for charging activity, consisting of 23.6 to 35.4% of their total
 322 “empty” miles traveled.

323 Not only do shorter range vehicles charge more frequently, simulation results in Table 2 also
 324 show that they utilize a smaller percent of their range before a charging event. The phenomenon
 325 of shorter-range vehicles recharging with higher baseline remaining range can be attributed to
 326 the demand-based charging strategy employed here, where a vehicle is assigned to charging
 327 status after rejecting a trip request due to insufficient range. With shorter ranges, the SAEVs are
 328 more frequently assigned to charging status due to increased probability of having insufficient
 329 range for trips. To explore whether charging less frequently would improve the fleet performance
 330 of the shorter range SAEV scenarios, scenarios incorporating both demand- (trip rejection) and
 331 distance- (maximum range threshold) based charging strategies were also run. Table 3 displays
 332 simulation results where SAEVs are assigned to charging status after the vehicle has rejected a
 333 trip due to insufficient range and met a maximum range threshold. Results show that combining
 334 demand-based charging with a 75% (60-mile) maximum range criteria yielded the best fleet
 335 performance metrics from a user perspective. Average wait times reduced to 7.37 minutes per
 336 trip and percent of trips unserved decreased to 1.70%, competitive with the SAV scenario results
 337 in Table 2. From the operator perspective, applying this charging strategy increases the necessary
 338 fleet size slightly (by 0.1%) and decreases induced travel by 12.7%. Increasingly stringent
 339 recharging distance criteria continually decreases induced VMT, primarily from reduction in
 340 relocation miles. However, as relocation miles decrease, induced miles to pick up travelers
 341 increase (and subsequently increases wait times), demonstrating the inherent tradeoffs between
 342 reducing extra VMT and enhancing user experience (as measured by wait times and percent of
 343 trips served).

344 **Table 3. Demand- and Distanced-Based Charging (SAEV with Level II Charging)**

Charging Strategy:	Recharge Upon Trip Rejection, Max Range=80 mi	Recharge Upon Trip Rejection, Max Range=60 mi	Recharge Upon Trip Rejection, Max Range=40 mi	Recharge Upon Trip Rejection, Max Range=20 mi
Fleet Size	57,279	57,354	57,278	57,174
% Trips Unserved	3.9%	1.7%	3.0%	3.4%
Avg Wait Time	8.1	7.4	8.2	8.5

(min)				
Avg Range Remaining at Recharge (mi)	43.0	22.2	13.2	6.4
% Total New Induced Travel	10.7%	9.3%	9.1%	9.0%
% New Induced Travel for Charging	2.5%	3.3%	3.1%	3.1%
% New Induced Travel for Relocation	4.1%	1.9%	1.6%	1.5%
% New Induced Travel for Trips	4.1%	4.1%	4.4%	4.5%

345 **FINANCIAL ANALYSIS**

346 Simulation results offer some insight into how combinations of vehicles and charging
347 infrastructure impact fleet operations, but a financial analysis is necessary to truly grasp the
348 tradeoff between additional capital investment (into vehicles with bigger batteries or more
349 expensive fast charging stations) and user benefits (measured in additional trips served or
350 decreased wait times). For each vehicle and charging station type, analysis was conducted for
351 three cost levels: low-, medium-, and high-cost scenarios, as shown in Table 4.

352 **Table 4. Vehicle & Charging Infrastructure Cost Assumptions**

	Low Cost	Mid Cost	High Cost
Vehicle Capital			
SAEV (per vehicle)	\$35,000	\$40,000	\$55,000
LR SAEV (per vehicle)	\$45,000	\$50,000	\$80,000
Replacement battery (per kWh)	\$240	\$405	\$570
Vehicle Operations			
Maintenance (per mile)	\$0.055	\$0.061	\$0.066
Insurance & Registration (per vehicle-year)	\$1,280	\$1,600	\$1,920
Electricity (per kWh)	\$0.11	\$0.13	\$0.26
Charging Infrastructure			
Level II Charging (per charger)	\$8,000	\$12,000	\$18,000
Level II Annual Maintenance (per charger)	\$25	\$40	\$50
Level III Charging (per charger)	\$10,000	\$45,000	\$100,000
Level III Annual Maintenance (per charger)	\$1,000	\$1,500	\$2,000

353

354 For vehicle capital costs, the non-autonomous SAEVs are assumed to cost from \$25,000 (similar
355 to Mitsubishi i-Miev and Smart Fortwo Electric Drive BEVs) to \$45,000 per vehicle
356 (approximate retail cost of BMW i3 BEV), with a most likely price of \$30,000 (comparable to
357 Nissan LEAF and Ford Focus Electric BEVs). The non-autonomous LR SAEVs are assumed to
358 cost between \$35,000 (projected price of the future 2017 Tesla Model 3 and Chevrolet Bolt) and
359 \$70,000 (retail price for the current model Tesla Model S), with a most likely price of \$40,000
360 per vehicle as critics believe the projected pricing for LR BEVs is too optimistic (see, e.g.

361 Anderman 2014). These vehicle costs do not consider government rebates and incentives for EV
 362 purchases. AV technology is assumed to add \$10,000 to the cost of each vehicle around the time
 363 AV technology first hits the commercial market in 2025, per estimates from IHS (2014) and
 364 Schultz (2014). To convert vehicle capital costs to a per-mile basis, each SAEV is assumed to be
 365 in operation for 231,000 miles before replacement, equivalent to the average life span of a New
 366 York City taxicab (New York City Taxi & Limousine Commission 2014). The battery is
 367 assumed to be replaced once during the SAEV’s service span (or per 115,500 miles), in line with
 368 most BEVs’ 100,000-mile battery warranties and evaluations of EV batteries (see, e.g., Knipe et
 369 al. 2003). Cost for replacement batteries (24 kWh for SAEVs and 60 kWh for LR SAEVs) are
 370 assumed to cost between \$380 to \$570 per kWh, per estimates from Plotkin and Singh (2009).

371 For vehicle operation costs, maintenance (including tires) is assumed to cost between 5.5 and 6.6
 372 cents per mile, similar to non-autonomous vehicles (AAA 2014). Insurance and registration are
 373 assumed to be on the order of two to three times the cost of privately owned vehicles, similar to
 374 assumptions in Burns et al. (2013), which translates to \$1,280 to \$1,920 annually (AAA 2014).
 375 Per-mile fuel costs assume electricity ranges 11 to 26 cents per kWh, with a mid-range cost of 13
 376 cents per kWh, the US national residential electricity average (EIA 2015). The high cost scenario
 377 allows flexibility in accommodating future variable priced electricity, a growing possibility with
 378 the introduction of smart metering technology.

379 For charging infrastructure, Level II chargers are assumed to cost between \$8,000 and \$18,000
 380 each, including costs for installation, hardware, materials, labor, and administration (Chang et al.
 381 2012, USDOE 2012). Annual maintenance cost for Level II chargers are assumed to be minimal
 382 at \$25 to \$50 per year (USDOE 2012). Level III chargers are assumed to range from \$10,000 to
 383 \$100,000, with average cost at \$45,000 per station (USDOE 2012, New York City Taxi &
 384 Limousine Commission 2013). This cost includes installation, hardware, materials, labor,
 385 administration, and transformer upgrades. Annual maintenance cost for Level III chargers are
 386 assumed to range from \$1000 to \$2000 (New York City Taxi & Limousine Commission 2013).
 387 To convert charging infrastructure to a per-mile basis, the service life span of charging stations is
 388 assumed to be 10 years (Chang et al. 2012). Table 5 breaks down the cost per occupied mile of
 389 travel (costs are incurred for total miles of travel but allocated to each occupied mile of travel)
 390 for each vehicle and charging infrastructure combination in the mid-cost scenario.

391 **Table 5. Equivalent Cost Per Occupied Mile Traveled (Mid-Cost Scenario)**

	SAEV	SAEV Fast Charge	LR SAEV	LR SAEV Fast Charge
Vehicle & Battery	\$0.249	\$0.250	\$0.346	\$0.346
Vehicle Maintenance	\$0.071	\$0.071	\$0.066	\$0.066
Insurance & Registration	\$0.038	\$0.026	\$0.025	\$0.020
Electricity	\$0.045	\$0.045	\$0.042	\$0.042
Charging Station Capital	\$0.015	\$0.030	\$0.007	\$0.004
Charging Station Maintenance	\$0.000	\$0.010	\$0.000	\$0.001
TOTAL	\$0.417	\$0.433	\$0.486	\$0.479

392

393 Under the most likely mid-cost scenario, a fleet of SAEVs or LR SAEVs can be operated at an
394 equivalent per-occupied-mile-traveled cost of \$0.42 to \$0.49. The most uncertain component of
395 this operating cost estimate is the AV technology. While \$10,000 per vehicle is assumed in the
396 base results in Table 5, the range of cost estimates of market-ready AV technology is large.
397 Various sources report the cost of the retrofitted AV technology on current Google self-driving
398 cars to range from \$75,000 to \$250,000 (Rogers 2015, Tannert 2014). Once the technology is
399 mature, IHS (2014) estimates AV technology will cost between \$3500 to \$5000 per vehicle after
400 5 to 10 years on the market. Incorporating the Table 4's mid-cost figures for all other cost
401 components, SAEV operation costs range from \$0.392 per mile when AV technology costs are
402 \$5000 per vehicle to \$0.867 per mile when AV technology costs are \$100,000 per vehicle.

403
404 Using APTA (2013) statistics, for a transit system that serves 2.4 billion annual passenger-miles,
405 general administration expenses (including facilities and salaries) add approximately \$0.184 to
406 per-mile operational costs. Assuming operating margins of 10% (similar to the transportation
407 industry average) and using mid-cost estimates from Table 4, SAEV service can be offered at
408 roughly \$0.66 to \$0.74 per occupied mile of travel. These costs are on the low end of current
409 manually-driven free-float carsharing services such as Car2Go, which charges roughly \$0.70 to
410 \$1.23 per mile in Austin, Texas (assuming trips are between 2 to 10 miles and travel speeds are
411 between 15 to 35 mph). Under this pricing assumption, SAEV users would pay roughly 21 to
412 49% of what is currently charged by transportation network companies like Uber and Lyft
413 (whose equivalent per-mile pricing is \$1.50 to \$3.18 in Austin). In fact, these costs are
414 competitive with AAA (2014) estimates of average costs of private vehicle ownership, which
415 ranges from \$0.40 to \$0.95 cents per mile depending on annual mileage and vehicle type,
416 suggesting that availability of a SAEV fleet can have significant impacts on private vehicle use
417 (and ownership), particularly for low-mileage households.

418 Cost estimates in Table 5 are derived from fleet size and induced VMT estimates with a demand-
419 based charging strategy with no maximum range restriction (Table 2). Adding a 75% maximum
420 range restriction (Table 3) on the SAEV base scenario reduces the cost by \$0.020 per mile,
421 yielding the most cost efficient scenario at \$0.397 per mile. It is worth noting that cost estimates
422 are based on traditional, wired charging infrastructure. Currently, a residential Level II wireless
423 (inductive) charger can deliver similar charge times as traditional corded units while costing
424 approximately \$2500 more per unit (Evatran n.d.). This translates to a minimal \$0.002 to \$0.003
425 increase in equivalent per-mile costs for the SAEV fleets modeled here. Level III inductive
426 chargers are not currently commercially available. If wireless charging is not available for the
427 SAEV fleets, an alternative would be to install traditional corded charging infrastructure and hire
428 charging station attendants at each of the 1500 some odd charging station sites. Assuming one
429 \$15-per-hour-wage attendant per charging station site, per-occupied-mile-traveled costs in Table
430 5 would increase \$0.077 to \$0.085.

431 While these per-mile costs are lower than current carsharing services and competitive with
432 private car ownership, their ability to compete with a fleet of non-electric SAVs depends on the
433 availability of wireless recharging infrastructure and government tax incentives on EV purchase
434 prices. Assuming SAVs utilize existing gasoline stations with no additional infrastructure
435 investment, a fleet of SAVs can be operated for \$0.400 per mile with a 231,000-mile vehicle life
436 span, \$30,000 per SAV purchase cost (\$20,000 for vehicle, \$10,000 for AV technology), 30 mpg
437 fuel economy, \$3.50 per gallon gasoline price, \$15 per hour wage per service attendant per

438 gasoline station, and the same AAA-based costs for maintenance, insurance, and registration
439 prescribed to SAEVs. Of course, this per-mile cost is highly sensitive to gasoline prices. With
440 EVs purchased at full price, SAEVs with wireless recharging are competitive with SAVs on a
441 per mile basis when gasoline is at \$3.50 per gallon. With current federal tax incentives of \$7500
442 per EV, SAEVs become price-competitive with SAVs when gasoline is at \$2.50 per gallon.
443 Without wireless recharging infrastructure (and using station attendants at charging sites),
444 SAEVs purchased with the \$7500 federal tax rebate are not price-competitive with SAVs until
445 gasoline reaches \$4.69 per gallon. Without the federal rebate, this increases to \$5.70 per gallon.

446 CONCLUSIONS

447 Motivated by natural synergies between autonomous driving technology and EVs in a shared
448 setting, this paper employs an agent-based model to simulate the operations of a fleet of SAEVs
449 in a medium-sized metropolitan area under various vehicle and infrastructure scenarios.
450 Simulation results show that fleet size is highly dependent on charging infrastructure and vehicle
451 range. For the non-electric SAV scenario, each shared vehicle can replace 7.3 private vehicles.
452 For a fleet of 80-mile range SAEVs with a 4 hour full recharge time, this replacement rate drops
453 to one shared vehicle for every 3.7 private vehicles, since more than half of the fleet is tied up in
454 charging activities during any time period. Simulation results also suggest these shared fleets can
455 serve 95.6 to 97.9% of all trips with average wait times between 7 and 10 minutes per trip, while
456 producing an additional 7 to 14% of “empty” VMT for traveling to passengers, strategic
457 repositioning, and accessing charging stations. While this induced travel can be reduced slightly
458 with strategic charging, model results also reveal the inherent tradeoffs between reduction of
459 induced “empty” travel and improvement of user experience (as measured by wait times and
460 percent of trips served). These tradeoffs highlight the need for a dynamic pricing scheme for
461 SAEVs which penalizes trips that incur more relocation miles (and thereby increase subsequent
462 trip wait times) and incentivize trips that coincide with strategic relocation (and thereby decrease
463 subsequent trip wait times).

464 Financial analysis reveals that despite requiring the largest fleet and the most charging stations,
465 the base 80-mile range SAEV fleet with Level II charging stations is the cheapest to operate on a
466 per-mile basis of all the EV scenarios. This is primarily due to the high sensitivity of per-mile
467 operating costs to vehicle purchase price (with SAEVs assumed to cost \$10,000 less per vehicle
468 compared to LR SAEVs in the mid-cost scenarios). While SAEVs with Level II charging
469 infrastructure is cost effective, the scenario is ineffective in spreading out charge demand, with
470 as much as 53% of the fleet concurrently charging during the peak charging period of the day. If
471 SAEVs become a widely adopted mode, this type of fleet can create significant demand on the
472 electric grid and necessitate large parking areas (stations) while charging during peak hours. LR
473 SAEVs with Level III fast charging infrastructure, while costing 14.9% more per mile compared
474 to SAEVs with Level II charging stations, is very effective at demand spreading, with only 7.6%
475 of the fleet concurrently charging during the peak charging period.

476 Financial analysis reveals that under the most likely scenario, a fleet of SAEVs can be operated
477 at \$0.41 to \$0.47 per occupied mile traveled. The competitiveness of SAEVs compared to non-
478 electric SAVs hinges almost singly on the availability of automated wireless charging. With
479 wireless automated charging, SAEVs can be price-competitive with SAVs when gasoline is

480 priced at \$3.50 per gallon or less. But with attendant serviced charging, SAEVs are only price
481 competitive with SAVs when gasoline reaches \$4.35 to \$5.70 per gallon.

482 The agent-based model presented here has limitations that merit improvement in future
483 applications of this type. First, the charging-station generation process mimics the objective of a
484 coverage model(see, e.g., Torgas et al., 1971), thereby ensuring full coverage of all charging
485 demand, but it does not consider budgetary constraints and allows for an unlimited number of
486 charging stations. Second, even though the Poisson-based trip generation process here introduces
487 some variation in specific cell trip generation rates, actual trip generation rates in real city
488 systems are significantly less regular, over space and over time. In exurban areas, an overall low
489 population density is often reflected by pockets of somewhat denser residential development
490 (planned developments, for example) among much larger areas of very little population. Lastly,
491 the scenarios modeled here assume that SAEVs will serve 10% of a region's trip demand and
492 that the temporal and spatial distributions of SAEV trips are the same as the region's overall trip-
493 making patterns. In reality, an SAEV's fleet metrics should be sensitive to trip demand density,
494 over space and time. Additionally, SAEV mode may be more attractive to specific types of trips,
495 rather than be equally appealing for all trips.

496 **ACKNOWLEDGEMENTS**

497 The authors are very grateful for National Science Foundation support for this research (in the
498 form of an IGERT Traineeship for the first author and Graduate Research Fellowship for the
499 third author), Dr. Daniel Fagnant's provision of the starting code, Prateek Bansal's assembly of
500 Austin's regional trip data, Dr. Peter Stone's editorial guidance, and Dave Tuttle's continued
501 alerts on relevant EV research.

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